



Fred T. Loomis

## TUG AND TOWED GLIDER RATE OF CLIMB

By R. D. HISCOCKS

It is often asked whether a certain airplane will safely tow a certain glider. Two of the most critical points are the rate of climb and the angle of climb of the airplane when used as a tug. In the following paper Mr. R. D. Hiscocks, a member of the Technical Committee of the Soaring Association of Canada gives a method for checking these points, which should be useful to gliding groups. B. S. Shenstone, President, Soaring Association of Canada.

*Ed: This paper represents a careful study of the physical requirements of aerotowing of gliders. It is most interesting to note that for a combination having a three to one ratio of gross weight of airplane to glider the maximum climb rate is reduced by only 30'/minute, from 750 to 720'/minute. Based on this study a revision and clarification of requirements for aerotow waivers appears to be in order.*

The purpose of this article is to outline an elementary method of calculating the rate and angle of climb of an aeroplane towing a glider.

It is convenient to begin with a fictitious number  $V_{cf}$  which is defined as the rate of climb which would be obtained if all the available power were used to overcome the force of gravity on the two aircraft, therefore:

$$\begin{aligned} V_{cf} &= 550 \text{ n.b.h.p.} \div W \\ n &= \text{propeller efficiency.} \\ \text{b.h.p.} &= \text{engine brake horsepower.} \\ W &= \text{total weight of glider and tug (lb.).} \end{aligned}$$

In a steady glide at a sinking speed  $V_s$  the two aircraft lose potential energy at the rate  $WV_s$ . Therefore the power required to maintain a fixed altitude is:

$$550 \text{ n.b.h.p.} = WV_s \quad (2)$$

If  $V$  is the velocity of the tug and glider along the flight path in a glide and  $L/D$  is the lift: drag ratio of the combination then is:

$$V_s = V \div L/D \quad (3)$$

Let the subscripts "a" and "g" refer to aeroplane and glider respectively, and  $V_{sa}$  and  $V_{sg}$  refer to the individual aeroplane and glider sinking speeds, then from Equation 3, by a little manipulation:

$$V_s = \frac{V}{W} \left( \frac{W_a}{(L/D)_a} + \frac{W_g}{(L/D)_g} \right) = \frac{W_a}{W} V_{sa} + \frac{W_g}{W} V_{sg} \quad (4)$$

If we define the aeroplane and glider fictitious sinking speeds as:

$$\begin{aligned} V_{saf} &= (W_a \div W) V_{sa} \\ V_{sgf} &= (W_g \div W) V_{sg} \end{aligned} \quad (5)$$

Equation 4 becomes simply:

$$V_s = V_{saf} + V_{sgf} \quad (6)$$

and equation 2 becomes:

$$550 \text{ n.b.h.p.} = W (V_{saf} + V_{sgf}) \quad (7)$$

When the engine delivers more power than is required for level flight, then the excess, which is available for climbing, is from Equation 7:

Excess Power =  $550 \text{ n.b.h.p.} - W (V_{saf} + V_{sgf})$   
or, dividing by the total weight, we obtain as the true rate of climb of the combination:

$$V_c = (550 \text{ n.b.h.p.} \div W) - (V_{saf} + V_{sgf})$$

or, from Equation 1:

$$V_c = V_{cf} - (V_{saf} + V_{sgf}) \quad (8)$$

The calculation of  $V_{cf}$  from Equation 1 will usually present little difficulty and a "speed polar" curve giving  $V_{sg}$  in terms of forward speed will normally be available for the glider. The remaining task then, in order